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### 1 Module Display\_hasse\_intf : Default specification for drawing with the DOT-utility.

```
module type DEFAULT_SPEC =
  sig
    DOT-options (see "man dot")
    val name : string
    val label : string
    val size_x : float
    val size_y : float
    val ratio : float
    val rotation : float
    val center : bool
    val top_attr : string
      Node attribute string for top nodes, e.g. "shape = box"
    val bot_attr : string
      Node attribute string for bottom nodes
    val top_bot_attr : string
      Node attribute string for top/bottom nodes
    val edge_attr : string
      Edge attribute string, e.g. "color = blue"
```

```

end

module type SPEC =
  sig

    include Display_hasse_intf.DEFAULT_SPEC

    type el
    type +'a node
    val pp_node_attr : Format.formatter ->
      el node -> unit

    pp_node_attr ppf node prints attributes of node to the pretty-printer ppf.

  end

```

Specification for drawing Hasse-diagrams.

```

module type DISPLAY_HASSE =
  sig

    type pomap
    val fprintf : Format.formatter -> pomap -> unit

    fprintf ppf pm prints partially ordered map pm to the pretty-printer ppf.

    val printf : pomap -> unit

    printf ppf pm prints partially ordered map pm to stdout.

  end

```

Interface for drawing Hasse-diagrams.

## 2 Module `Display_hasse_impl` : Default specification than can be used by the pretty-printer for Hasse-diagrams.

Just `include` it into some module and override the defaults as required.

```

module DefaultSpec :
  sig

    include DEFAULT_SPEC
    val pp_node_attr : Format.formatter -> 'a -> unit
  end

```

Default specification than can be used by the pretty-printer for Hasse-diagrams. Just `include` it into some module and override the defaults as required.

```

module Make :
  functor (POMap : Pomap_intf.POMAP) -> functor (Spec : SPEC with type (+'a) node
= 'a POMap.node) -> DISPLAY_HASSE with type pomap = Spec.el POMap.pomap

```

Functor that generates a pretty-printer for Hasse-diagrams from a partially ordered map and a pretty-printer specification. See the `Display_hasse_intf.DISPLAY_HASSE[1]`-interface for documentation.

### 3 Module Store\_intf : Specification of indices used to index elements in stores

```

module type INDEX =
sig
  type t
    Type of indices

  type gen
    Type of index generators

  module Set :
    Set.S with type elt = t
    Efficient sets of indices

  module Map :
    Map.S with type key = t
    Efficient maps of indices

  val start : gen
    The start state of the index generator

  val next_ix : gen -> t
    next_ix gen
    Returns the next index that generator gen will produce.

  val next : gen -> t * gen
    next gen
    Returns the tuple of (new_ix, new_gen), where new_ix is the next index and
    new_gen the next state of the index generator.

  val remove_ix : gen -> t -> gen

```

```

remove_ix gen_ix
Returns an updated index generator which is guaranteed to never return index ix or
any other previously returned index.

val int_of_ix : t -> int
    int_of_ix ix converts index ix to an integer.
    Raises Failure if index out of range for machine integers.

end

module type STORE =
sig
  module Ix :
    Store_intf.INDEX
      Index module used to index elements in the store

  type +'a t
    Type of stores

  val empty : 'a t
    The empty store

  val is_empty : 'a t -> bool
    is_empty s
    Returns true if s is empty, false otherwise.

  val cardinal : 'a t -> int
    cardinal s
    Returns the number of elements in s.

  val next_ix : 'a t -> Ix.t
    next_ix s
    Returns the next index the store s will use to index a new element.

  val singleton : 'a -> Ix.t * 'a t
    singleton el
    Returns the tuple (ix, store), where ix is the index under which the only element
el was stored, and store is the store containing el.

  val add : 'a -> 'a t -> Ix.t * 'a t

```

add el s

**Returns** the tuple (new\_ix, new\_store), where new\_ix is the index under which the new element el was stored, and new\_store is the new store containing el.

val find : Ix.t -> 'a t -> 'a

find ix s

**Raises** Not\_found if index ix not bound.

**Returns** the element stored under index ix.

val update : Ix.t -> 'a -> 'a t -> 'a t

update ix el s rebinds index ix in store s to point to el, and returns the resulting store. The previous binding disappears. New indices resulting from further adds are guaranteed to have higher indices.

**Raises** Not\_found if index ix not bound.

val remove : Ix.t -> 'a t -> 'a t

remove ix s removes the binding of index ix of store s, and returns the resulting store.

val iter : ('a -> unit) -> 'a t -> unit

iter f s applies f to all stored elements in store s. The order in which elements are passed to f is unspecified.

val iteri : (Ix.t -> 'a -> unit) -> 'a t -> unit

iteri f s applies f to all indexes and their related elements in store s. The order in which elements are passed to f is unspecified.

val map : ('a -> 'b) -> 'a t -> 'b t

map f s

**Returns** a store with all elements in s mapped from their original value to the codomain of f. Only the elements are passed to f. The order in which elements are passed to f is unspecified.

val mapi : (Ix.t -> 'a -> 'b) -> 'a t -> 'b t

mapi f s same as map, but function f also receives the index associated with the elements.

val fold : ('a -> 'b -> 'b) -> 'a t -> 'b -> 'b

fold f s a computes (f eN ... (f e1 a) ...), where e1 ... eN are the elements of all bindings in store s. The order in which the bindings are presented to f is unspecified.

val foldi : (Ix.t -> 'a -> 'b -> 'b) -> 'a t -> 'b -> 'b

`foldi f s` a same as `fold`, but function `f` also receives the index associated with the elements.

`val to_list : 'a t -> (Ix.t * 'a) list`

`to_list s` converts `s` to an association list of indices and elements.

`val choose : 'a t -> Ix.t * 'a`

`choose s`

**Raises** `Not_found` if `s` is empty.

**Returns** a tuple `(ix, x)`, where `ix` is the index of some unspecified value `x` in store `s`.

`val filter : (Ix.t -> 'a -> bool) -> 'a t -> 'a t`

`filter p s`

**Returns** the store of all elements in `s` that satisfy `p`.

`val partition : (Ix.t -> 'a -> bool) ->`  
`'a t -> 'a t * 'a t`

`partition p s`

**Returns** a pair of stores `(s1, s2)`, where `s1` is the store of all the elements of `s` that satisfy the predicate `p`, and `s2` is the store of all the elements of `s` that do not satisfy `p`.

`val eq_classes : ('a -> 'a -> bool) ->`  
`'a t -> ('a * 'a t) list`

`eq_classes eq s`

**Returns** a list of tuples `(el, ec)`, where `el` is the only kind of element as identified by the equivalence relation `eq` stored in the equivalence class (store) `ec` under each index. Every such equivalence class is unique and maximal with respect to `s`, and the original indices of the elements are preserved in each class.

`val get_ix_map : 'a t -> 'a Ix.Map.t`

`get_ix_map s`

**Returns** a map of all indices mapped to their respective elements in store `s`.

`end`

Interface to stores

## 4 Module Store\_Impl : Implementation of stores

Implementation of stores

```
module IntIx :  
  Store_intf.INDEX  
  
module Make :  
  functor (Ix : Store_intf.INDEX) -> Store_intf.STORE  
  
module IntStore :  
  Store_intf.STORE
```

## 5 Module Pomap\_intf : Specification of a partial order relation

```
module type PARTIAL_ORDER =  
  sig
```

type el  
 Element type

type ord =  
 | Unknown  
 | Lower  
 | Equal  
 | Greater

val compare : el ->  
 el -> ord

end

```
module type POMAP =  
  sig
```

Modules and types

module Store :  
 Store\_intf.STORE

Store module used to store nodes of the partially ordered map.

type key

Type of map keys

type +'a node

Type of nodes in the partially ordered map

```
type +'a pomap
```

Type of partially ordered maps

```
type 'a add_find_result =
| Found of Store.Ix.t * 'a node
| Added of Store.Ix.t * 'a node * 'a pomap
```

Type of result originating from an `add_find` operation

Map-constructors

```
val empty : 'a pomap
```

The empty partially ordered map.

```
val singleton : key -> 'a -> 'a pomap
```

```
singleton k el
```

**Returns** a partially ordered map containing as only binding the one from `k` to `el`.

Information on maps

```
val is_empty : 'a pomap -> bool
```

`is_empty pm` tests whether partially ordered map `pm` is empty.

```
val cardinal : 'a pomap -> int
```

```
cardinal pm
```

**Returns** the number of elements in `pm`.

Adding and removing

```
val add : key ->
  'a -> 'a pomap -> 'a pomap
```

```
add k el pm
```

**Returns** a partially ordered map containing the same bindings as `pm`, plus a binding of `k` to `el`. If `k` was already bound in `pm`, its previous binding disappears.

```
val add_node : 'a node ->
  'a pomap -> 'a pomap
```

```
add_node node pm
```

**Returns** a partially ordered map containing the same bindings as `pm` plus a binding as represented by `node`. If the associated key already existed in `pm`, its previous binding disappears.

```
val remove : key ->
  'a pomap -> 'a pomap
```

`remove k pm`

**Returns** a map containing the same bindings as `pm` except for the node with key `k`.

`val remove_node : 'a node ->`  
`'a pomap -> 'a pomap`

`remove_node node pm`

**Returns** a map containing the same bindings as `pm` except for the one with the key of `node`.

`val remove_ix : Store.Ix.t -> 'a pomap -> 'a pomap`

`remove_ix ix pm`

**Raises** `Not_found` if `ix` does not index any node.

**Returns** a map containing the same bindings as `pm` except for the node indexed by `ix`.

`val take : key ->`  
`'a pomap ->`  
`Store.Ix.t * 'a node * 'a pomap`

`take k pm`

**Raises** `Not_found` if there is no binding for `key`.

**Returns** a tuple `(ix, node, map)`, where `ix` is the index of the `node` associated with key `k` in `pm`, and `map` is `pm` without this element.

`val take_ix : Store.Ix.t ->`  
`'a pomap ->`  
`'a node * 'a pomap`

`take_ix ix pm`

**Raises** `Not_found` if `ix` does not index any node.

**Returns** a tuple `(n, m)`, where `n` is the node associated with index `ix`, and `m` is a map without this element.

`val add_find : key ->`  
`'a -> 'a pomap -> 'a add_find_result`

`add_find k el pm` similar to `add`, but if the binding did already exist, then `Found (ix, node)` will be returned to indicate the index and node under which key `k` is bound. Otherwise `Added (new_ix, new_pm)` will be returned to indicate that `k` was bound under new index `new_ix` in the partially ordered map `new_pm`.

`val add_fun : key ->`  
`'a -> ('a -> 'a) -> 'a pomap -> 'a pomap`

`add_fun k el f pm` similar to `add`, but if the binding already existed, then function `f` will be applied to the previously bound data. Otherwise the binding will be added as in `add`.

Scanning and searching

`val mem : key -> 'a pomap -> bool`

`mem k pm`

**Returns** true if pm contains a binding for key k and false otherwise.

`val mem_ix : Store.Ix.t -> 'a pomap -> bool`

`mem el pm`

**Returns** true if pm contains a binding for data element el and false otherwise.

`val find : key ->`

`'a pomap -> Store.Ix.t * 'a node`

`find k pm`

**Raises** Not\_found if no such binding exists.

**Returns** a tuple (ix, node), where ix is the index of key k and node its associated node in map pm.

`val find_ix : Store.Ix.t -> 'a pomap -> 'a node`

`find_ix ix pm`

**Raises** Not\_found if such a node does not exist.

**Returns** the node associated with index ix in map pm.

`val choose : 'a pomap -> Store.Ix.t * 'a node`

`choose pm`

**Raises** Not\_found if pm is empty.

**Returns** a tuple (ix, node), where ix is the index of the node of some unspecified element in pm.

`val filter : (Store.Ix.t -> 'a node -> bool) ->`

`'a pomap -> 'a pomap`

`filter p pm`

**Returns** the map of all elements in pm that satisfy p.

`val partition :`

`(Store.Ix.t -> 'a node -> bool) ->`

`'a pomap ->`

`'a pomap * 'a pomap`

`partition p pm`

**Returns** a pair of maps (pm1, pm2), where pm1 is the map of all the elements of pm that satisfy the predicate p, and pm2 is the map of all the elements of pm that do not satisfy p.

## Iterators

```
val iter : ('a node -> unit) -> 'a pomap -> unit
```

`iter f pm` applies `f` to all bound nodes in map `pm`. The order in which the nodes are passed to `f` is unspecified. Only current bindings are presented to `f`: bindings hidden by more recent bindings are not passed to `f`.

```
val iteri : (Store.Ix.t -> 'a node -> unit) ->  
'a pomap -> unit
```

`iteri f pm` same as `Pomap_intf.POMAP.iter[5]`, but function `f` also receives the index associated with the nodes.

```
val map : ('a node -> 'b) ->  
'a pomap -> 'b pomap
```

`map f pm`

**Returns** a map with all nodes in `pm` mapped from their original value to identical nodes whose data element is in the codomain of `f`. The order in which nodes are passed to `f` is unspecified.

```
val mapi : (Store.Ix.t -> 'a node -> 'b) ->  
'a pomap -> 'b pomap
```

`mapi f pm` same as `Pomap_intf.POMAP.map[5]`, but function `f` also receives the index associated with the nodes.

```
val fold : ('a node -> 'b -> 'b) ->  
'a pomap -> 'b -> 'b
```

`fold f pm a` computes  $(f \ n_N \dots \ (f \ n_1 \ a) \ \dots)$ , where  $n_1 \dots \ n_N$  are the nodes in map `pm`. The order in which the nodes are presented to `f` is unspecified.

```
val foldi : (Store.Ix.t -> 'a node -> 'b -> 'b) ->  
'a pomap -> 'b -> 'b
```

`foldi f pm a` same as `Pomap_intf.POMAP.fold[5]`, but function `f` also receives the index associated with the nodes.

```
val topo_fold : ('a node -> 'b -> 'b) ->  
'a pomap -> 'b -> 'b
```

`topo_fold f pm a` computes  $(f \ n_N \dots \ (f \ n_1 \ a) \ \dots)$ , where  $n_1 \dots \ n_N$  are the nodes in map `pm` sorted in ascending topological order. Slower than `fold`.

```
val topo_foldi :  
(Store.Ix.t -> 'a node -> 'b -> 'b) ->  
'a pomap -> 'b -> 'b
```

`topo_foldi f pm a` same as `Pomap_intf.POMAP.topo_fold[5]`, but function `f` also receives the index associated with the nodes.

```

val topo_fold_ix : (Store.Ix.t -> 'a -> 'a) -> 'b pomap -> 'a -> 'a
topo_fold_ix f pm a same as Pomap_intf.POMAP.topo_fold[5], but function f only
receives the index associated with the nodes.

val rev_topo_fold : ('a node -> 'b -> 'b) ->
'a pomap -> 'b -> 'b
rev_topo_fold f pm a computes (f nN ... (f n1 a) ...), where n1 ... nN are
the nodes in map pm sorted in descending topological order. Slower than fold.

val rev_topo_foldi :
(Store.Ix.t -> 'a node -> 'b -> 'b) ->
'a pomap -> 'b -> 'b
rev_topo_foldi f pm a same as Pomap_intf.POMAP.rev_topo_fold[5], but function f
also receives the index associated with the nodes.

val rev_topo_fold_ix : (Store.Ix.t -> 'a -> 'a) -> 'b pomap -> 'a -> 'a
rev_topo_fold_ix f pm a same as Pomap_intf.POMAP.rev_topo_fold[5], but
function f only receives the index associated with the nodes.

val chain_fold : ('a node list -> 'b -> 'b) ->
'a pomap -> 'b -> 'b
chain_fold f pm a computes (f cN ... (f c1 a) ...), where c1 ... cN are the
ascending chaines of nodes in map pm. Only useful for small maps, because of
potentially exponential complexity.

val chain_foldi :
((Store.Ix.t * 'a node) list -> 'b -> 'b) ->
'a pomap -> 'b -> 'b
chain_foldi f pm a same as Pomap_intf.POMAP.chain_fold[5], but function f
receives chains including the index associated with the nodes.

val rev_chain_fold : ('a node list -> 'b -> 'b) ->
'a pomap -> 'b -> 'b
rev_chain_fold f pm a computes (f cN ... (f c1 a) ...), where c1 ... cN
are the descending chaines of nodes in map pm. Only useful for small maps, because of
potentially exponential complexity.

val rev_chain_foldi :
((Store.Ix.t * 'a node) list -> 'b -> 'b) ->
'a pomap -> 'b -> 'b
rev_chain_foldi f pm a same as Pomap_intf.POMAP.rev_chain_fold[5], but
function f receives chains including the index associated with the nodes.

```

Set-like map-operations

```
val union : 'a pomap ->  
  'a pomap -> 'a pomap
```

union pm1 pm2 merges pm1 and pm2, preserving the bindings of pm1.

```
val inter : 'a pomap ->  
  'a pomap -> 'a pomap
```

inter pm1 pm2 intersects pm1 and pm2, preserving the bindings of pm1.

```
val diff : 'a pomap ->  
  'a pomap -> 'a pomap
```

diff pm1 pm2 removes all elements of pm2 from pm1.

Node-creators and accessors

```
val create_node : key ->  
  'a -> Store.Ix.Set.t -> Store.Ix.Set.t -> 'a node
```

create\_node k el sucs prds

**Returns** a node with key k, data element el, successors sucs and predecessors prds.

```
val get_key : 'a node -> key
```

get\_key n

**Returns** the key associated with node n.

```
val get_el : 'a node -> 'a
```

get\_el n

**Returns** the data element associated with node n.

```
val get_sucs : 'a node -> Store.Ix.Set.t
```

get\_sucs n

**Returns** the successors associated with node n.

```
val get_prds : 'a node -> Store.Ix.Set.t
```

get\_prds n

**Returns** the predecessors associated with node n.

```
val set_key : 'a node -> key -> 'a node
```

set\_key n k sets the key of node n to k and returns new node.

```
val set_el : 'a node -> 'a -> 'a node
```

set\_el n el sets the data element of node n to el and returns new node.

```

val set_sucs : 'a node -> Store.Ix.Set.t -> 'a node
    set_sucs n sucs set the successors of node n to sucs and returns new node.

val set_prds : 'a node -> Store.Ix.Set.t -> 'a node
    set_prds n prds set the predecessors of node n to prds and returns new node.

Map-accessors

val get_nodes : 'a pomap -> 'a node Store.t
    get_nodes pm
Returns the store of nodes associated with partially ordered map pm. This store represents the Hasse-graph of the nodes partially ordered by their keys.

val get_top : 'a pomap -> Store.Ix.Set.t
    get_top pm
Returns the set of node indices of nodes that are greater than any other node in pm but themselves.

val get_bot : 'a pomap -> Store.Ix.Set.t
    get_bot pm
Returns the set of node indices of nodes that are lower than any other node in pm but themselves.

Operations over equivalences of data elements

val remove_eq_prds : ('a -> 'a -> bool) -> 'a pomap -> 'a pomap
    remove_eq_prds eq pm
Returns a map containing the same bindings as pm except for nodes whose non-empty predecessors all have the same data element as identified by eq.

val fold_eq_classes :
    ('a -> 'a -> bool) ->
    ('a -> 'a pomap -> 'b -> 'b) ->
    'a pomap -> 'b -> 'b
    fold_eq_classes eq f pm a factorizes pm into maximal equivalence classes of partial orders: all bindings in each class have equivalent data elements as identified by eq and are connected in the original Hasse-diagram. This function then computes (f ec_elN ecN ... (f ec_el1 ec1 a)), where ec1 ... ecN are the mentioned equivalence classes in unspecified order, and ec_el1 ... ec_elN are their respective common data elements.

val fold_split_eq_classes :
    ('a -> 'a -> bool) ->
    ('a -> 'a pomap -> 'b -> 'b) ->
    'a pomap -> 'b -> 'b

```

`fold_split_eq_classes` eq f pm a same as `Pomap_intf.POMAP.fold_eq_classes`[5], but the equivalence classes are split further so that no element of other classes would fit between its bottom and top elements. It is unspecified how non-conflicting elements are assigned to upper or lower classes!

```
val preorder_eq_classes : ('a -> 'a -> bool) ->
  'a pomap -> 'a pomap list
```

`preorder_eq_classes` eq pm

**Returns** a preordered list of equivalence classes, the latter being defined as in `fold_split_eq_classes`.

```
val topo_fold_reduced :
  ('a -> 'a -> bool) ->
  ('a node -> 'b -> 'b) ->
  'a pomap -> 'b -> 'b
```

`topo_fold_reduced` eq f pm a computes  $(f \ nN \dots \ (f \ n1 \ a) \dots)$ , where  $n1 \dots \ nN$  are those nodes in map pm sorted in ascending topological order, whose data element is equivalent as defined by `eq` to the one of lower elements if there are no intermediate elements that violate this equivalence.

Unsafe operations - USE WITH CAUTION!

```
val unsafe_update : 'a pomap ->
  Store.Ix.t -> 'a node -> 'a pomap
```

`unsafe_update` pm ix node updates the node associated with node index ix in map pm with node. The Hasse-diagram associated with the partially ordered map pm may become inconsistent if the new node violates the partial order structure. This can lead to unpredictable results with other functions!

```
val unsafe_set_nodes : 'a pomap ->
  'a node Store.t -> 'a pomap
```

`unsafe_set_nodes` pm s updates the node store associated with map pm with s. This assumes that s stores a consistent Hasse-diagram of nodes.

```
val unsafe_set_top : 'a pomap -> Store.Ix.Set.t -> 'a pomap
```

`unsafe_set_top` pm set updates the index of top nodes in map pm with set. This assumes that the nodes referenced by the node indices in set do not violate the properties of the Hasse-diagram of pm.

```
val unsafe_set_bot : 'a pomap -> Store.Ix.Set.t -> 'a pomap
```

`unsafe_set_bot` pm set updates the index of bottom nodes in map pm with set. This assumes that the nodes referenced by the node indices in set do not violate the properties of the Hasse-diagram of pm.

```
end
```

```
Interface to partially ordered maps
```

## 6 Module Pomap\_impl : Implementation of partially ordered maps

```
Implementation of partially ordered maps
```

```
module Make :  
  functor (PO : Pomap_intf.PARTIAL_ORDER) -> POMAP with type key = PO.el
```